

## 5.4A Graphing Quadratic Inequalities

#1 – 3: Determine whether each of the given points is a solution to the given quadratic inequality.

1.  $y \geq x^2 - 3x + 3$

a) (0,0)

$0 \geq (0)^2 - 3(0) + 3$

$0 \geq 3$  False

NOT a SOLN

b) (1,1)

$1 \geq (1)^2 - 3(1) + 3$

$1 \geq 1$  TRUE

SOLN

2.  $y < -\frac{1}{2}x^2 - x + 6$

a) (0,0)

$0 < -\frac{1}{2}(0)^2 - 0 + 6$

$0 < 6$  True

SOLN

b) (3,3)

$3 < -\frac{1}{2}(3)^2 - (3) + 6$

$< -\frac{9}{2} - 3 + 6$

$3 < -1\frac{1}{2}$  False

NOT SOLN

3.  $y > 2x^2 - x + 4$

a) (0,0)

$0 > 2(0)^2 - 0 + 4$

$0 > 4$  False

NOT SOLN

b) (1,5)

$5 > 2(1)^2 - (1) + 4$

$5 > 5$  False

NOT SOLN

#4 – 6: For each inequality and graph (the points plotted are points that exist on the boundary)...

- determine whether the boundary is included as a solution (solid) or not included as part of the solution (dashed).

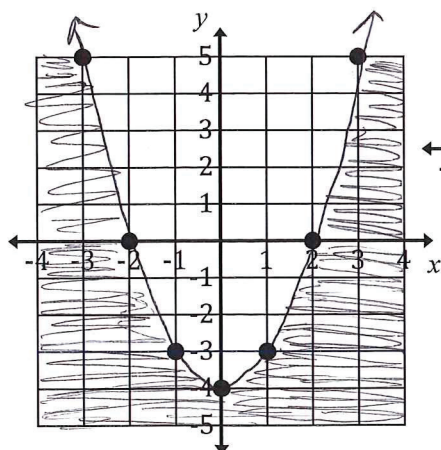
- use a test point to determine the solution region.

Graph the solution to each inequality.

4.  $y \leq x^2 - 4$

use (0,0)

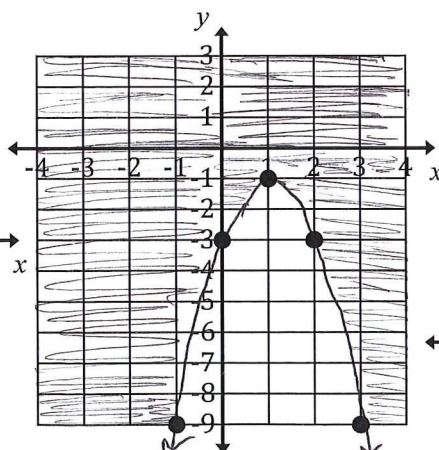
$0 \leq -4$  False



5.  $y \geq -2x^2 + 4x - 3$

use (0,0)

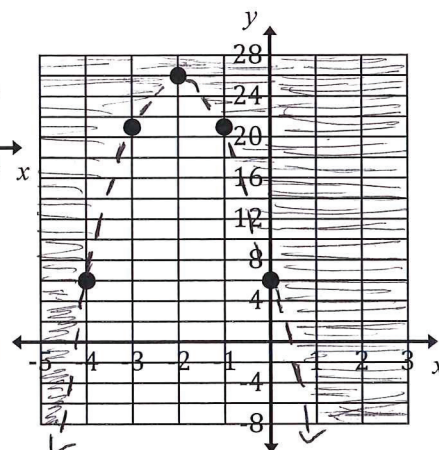
$0 \geq -3$  True



6.  $y > -5x^2 - 20x + 6$

use (0,0)

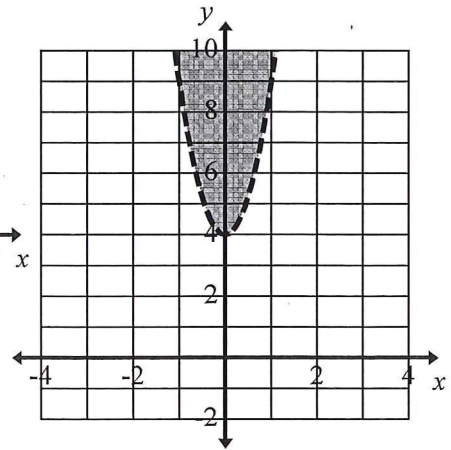
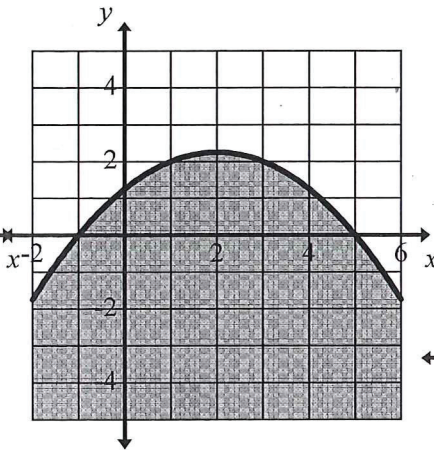
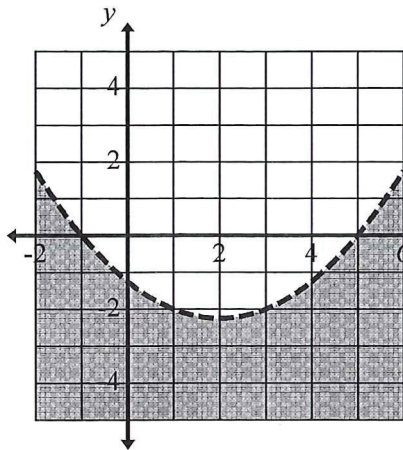
$0 > 6$  False



# 5.4A Graphing Quadratic Inequalities

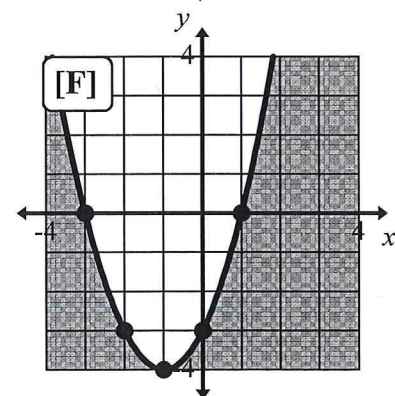
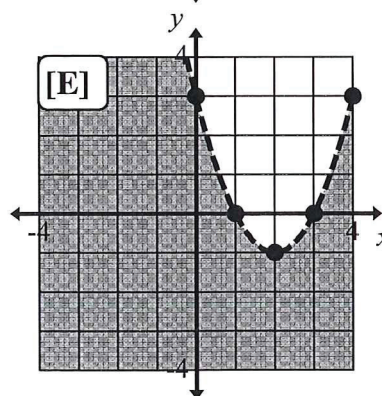
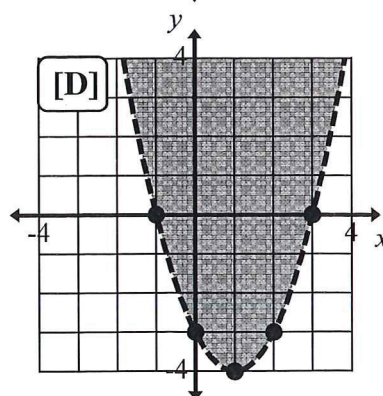
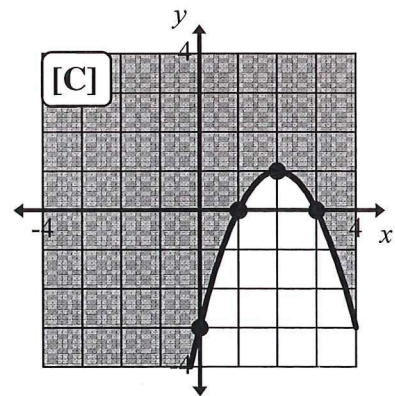
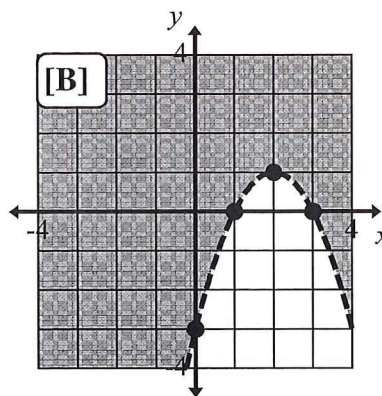
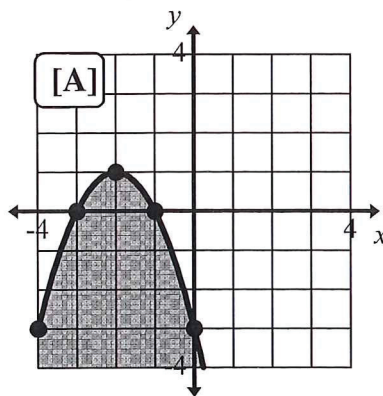
#7 – 9: Fill in the blank with the appropriate inequality sign.

7.  $y$   $\boxed{<}$   $\frac{1}{4}x^2 - 1x - \frac{5}{4}$       8.  $y$   $\boxed{\leq}$   $-\frac{1}{4}x^2 - 1x - \frac{5}{4}$       9.  $y$   $\boxed{>}$   $5x^2 + 4$



#10 – 15: Match the inequality with its graph.

C 10.  $y \geq -x^2 + 4x - 3$       A 11.  $y \leq -x^2 - 4x - 3$       F 12.  $y \leq x^2 + 2x - 3$   
E 13.  $y < x^2 - 4x + 3$       B 14.  $y > -x^2 + 4x - 3$       D 15.  $y > x^2 - 2x - 3$



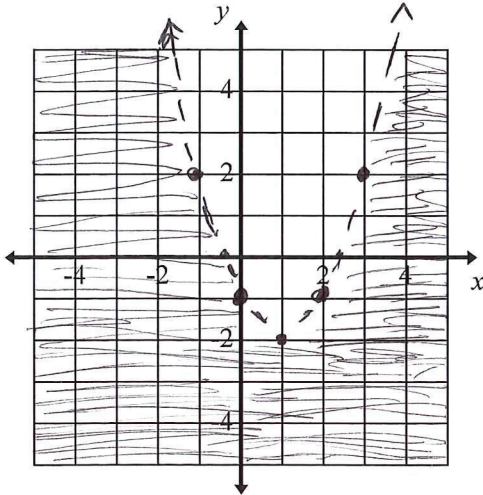


## 5.4A Graphing Quadratic Inequalities

#16 – 23: Draw the graph of each quadratic inequality. When graphing the boundary, consider the various forms of a quadratic and the significant features that are identified from each form.

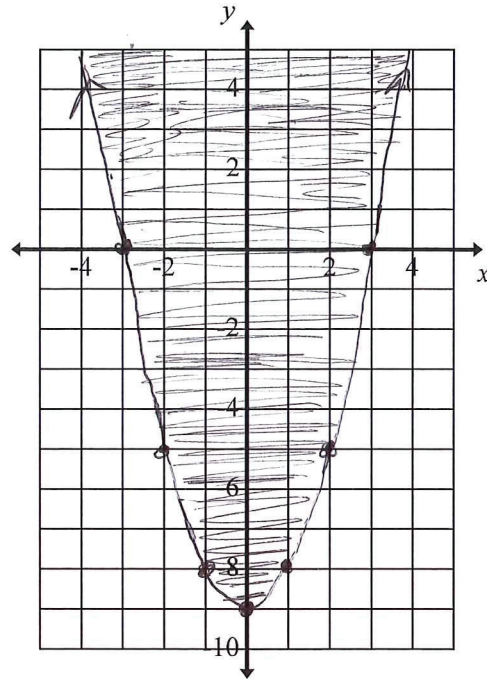
16.  $y < x^2 - 2x - 1$

$$\begin{aligned} x^2 - 2x &= 1 \\ x^2 - 2x + 1 &= 1 + 1 \\ \sqrt{(x-1)^2} &= \sqrt{2} \\ |x-1| &= \sqrt{2} \\ x-1 &= \pm\sqrt{2} \\ x &= 1 \pm \sqrt{2} \approx 2.41, -0.41 \end{aligned}$$



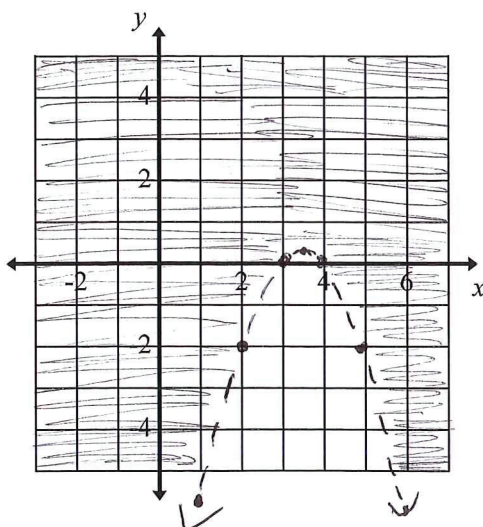
17.  $y \geq x^2 - 9$

$$\begin{aligned} (x+3)(x-3) \\ x = -3, x = 3 \end{aligned}$$



18.  $y > -x^2 + 7x - 12$

$$\begin{aligned} 0 &= -1(x^2 - 7x + 12) \\ 0 &= -1(x-3)(x-4) \\ x &= 3, x = 4 \end{aligned}$$



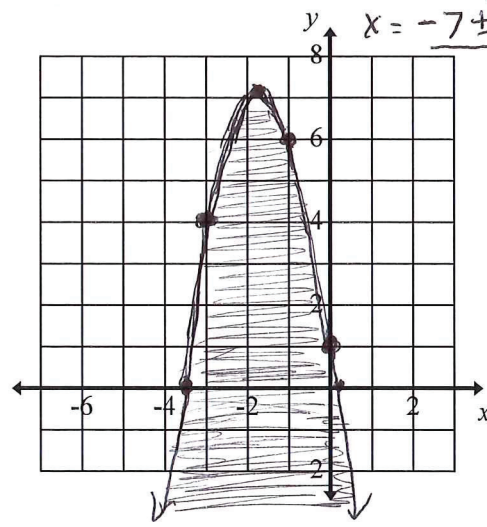
19.  $y \leq -2x^2 - 7x + 1$

$$a = -2 \quad b = -7 \quad c = 1$$

$$x = \frac{7 \pm \sqrt{(-7)^2 - 4(-2)(1)}}{2(-2)}$$

$$x = \frac{7 \pm \sqrt{57}}{-4}$$

$$x = \frac{-7 \pm \sqrt{57}}{4} \approx 0.14, -3.64$$



# 5.4A Graphing Quadratic Inequalities

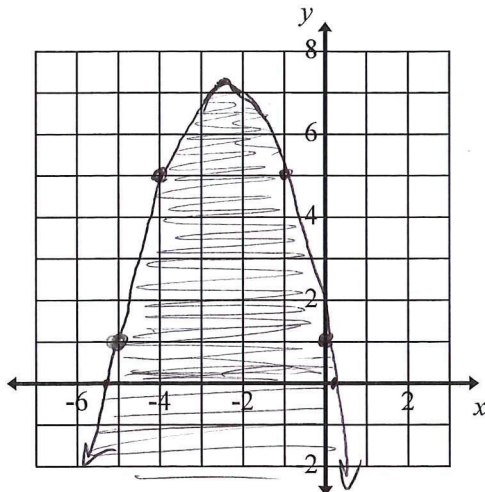
#16 – 23 (continued): Draw the graph of each quadratic inequality. When graphing the boundary, consider the various forms of a quadratic and the significant features that are identified from each form.

20.  $y \leq -x^2 - 5x + 1$

$a = -1$   
 $b = -5$   
 $c = 1$

$$x = \frac{5 \pm \sqrt{(-5)^2 - 4(-1)(1)}}{2(-1)}$$

$$x = \frac{5 \pm \sqrt{29}}{-2} \rightarrow -5.19, 0.19$$



21.  $y > \frac{1}{2}(x+6)^2 - 3$

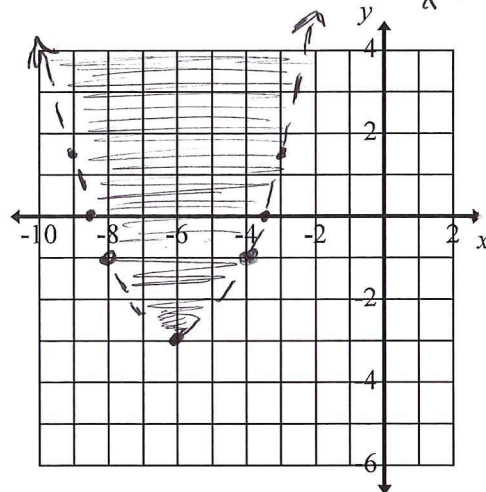
$$\frac{1}{2}(x+6)^2 - 3 = 0$$

$$\frac{1}{2}(x+6)^2 = 3$$

$$\sqrt{\frac{1}{2}(x+6)^2} = \sqrt{6}$$

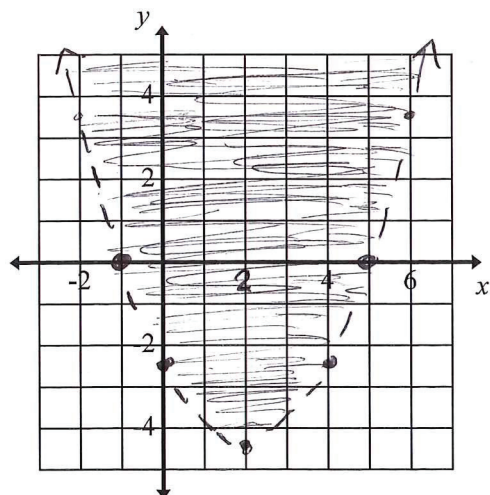
$$|x+6| = \sqrt{6}$$

$$x = -6 \pm \sqrt{6} \rightarrow -3.55, -8.44$$



22.  $y > \frac{1}{2}(x+1)(x-5)$

$x = -1, x = 5$



23.  $y \leq -2(x+1)^2 + 6$

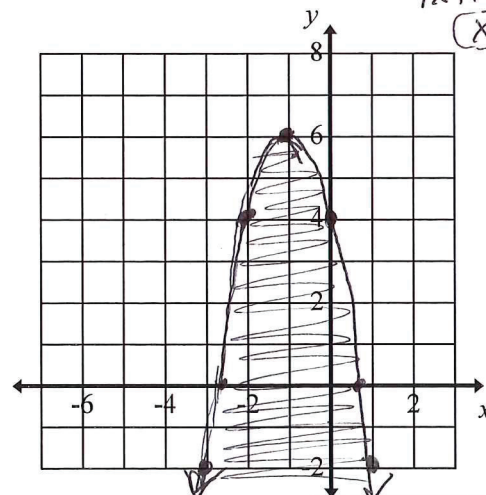
$$-2(x+1)^2 + 6 = 0$$

$$-2(x+1)^2 = -6$$

$$\sqrt{-2(x+1)^2} = \sqrt{6}$$

$$|x+1| = \sqrt{6}$$

$$x = -1 \pm \sqrt{6} \rightarrow 0.73, -2.73$$



Section 5.4A